

# Attribute-Based Certificateless Cryptographic System

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**Abstract**—As an extension of identity-based encryption scheme, attribute-based encryption scheme also has the key escrow problem. Multi-authority attribute-based encryption schemes are principal solution, but it is at the cost of the introducing extra infrastructure and communication.

This paper introduces the concept of attribute-based certificateless encryption system (ABCE), which is a new approach to mitigate the key escrow problem in attribute-based encryption scheme. In ABCE, the user can choose his own secret key that the KGC cannot obtain. In contrast to attribute-based encryption scheme under multiple authorities, our approach needs less extra cost. Following, we give a generic construction and an improvement in the efficiency.

**Index Terms**—certificateless cryptography, attribute-based encryption,  $k$ -sibling interactive function family, one-way function.

## I. INTRODUCTION

Sahai and Waters [2] introduced the concept of attribute-based encryption (ABE). Two variants of ABE were subsequently proposed. In the key-policy variant (KP-ABE) of Goyal, Pandey, Sahai and Waters (GPSW)[3], every ciphertext is associated with a set of attributes, and every user secret key is associated with a threshold access structure on attributes. Decryption is enabled if and only if the ciphertext attribute set satisfies the access structure on the user secret key. In the ciphertext-policy variant (CP-ABE) of Bethencourt, Sahai and Waters (BSW) [4], the situation is reversed: attributes are associated with user secret keys and access structures with ciphertexts. Following, in order to make the access structure more expressive, many schemes have been presented [2, 3, 5, 6, 7, 8, 9, 10]. Simultaneously, schemes [7, 11, 12, and 13] are devoted to get constant-size ciphertexts.

Similar to identity-based encryption schemes, the KGC is able to compute the private key corresponding to any attribute, and he is free to engage in malicious activities without any risk of being confronted in a court of law. The malicious activities could include: decrypting and reading messages meant for any user, which is called the key escrow problem. One approach to mitigate the key

escrow problem is to employ multi-authority attribute-based encryption, which allow the sender to specify for each authority  $k$  a set of attributes monitored by that authority and a number  $d_k$  so that the message can be decrypted only by a user who has at least  $d_k$  of the given attributes from every authority. Multi-authority attribute-based encryption is an attractive solution and successfully avoids placing trust in a single entity by making the system distributed. However, it is burdensome for a user to go to several key authorities, prove his attributes to each of them and get the corresponding private key component (which has to be done over a secure channel). Building on the ideas from [14], Chase proposed a solution for multi-authority attributes-based encryption, provided that a trusted central authority is available [15], but a global identifier is a "linchpin" for tying users' keys together. Her system relied on a central authority and was limited to expressing a strict "AND" policy over a pre-determined set of authorities. Müller, Katzenbeisser, and Eckert [16, 17] give a system with a centralized authority that realizes any LSSS access structure. Their construction builds on the Waters system; their proof is limited to non-adaptive queries. The system achieves roughly the same functionality as the engineering approach above, except one can still acquire attributes from additional authorities without revisiting the central authority. The scheme [18] removed the central authority using a distributed PRF; However, the same limitations of an AND policy of a determined set of authorities remained. Lin ET. al. [17] gives a threshold-based scheme that is also somewhat decentralized. The set of authorities is fixed ahead of time, and they must interact during the system setup. The system is only secure up to collusions of  $m$  users, where  $m$  is a system parameter chosen at setup such that the cost of operations and key storage scales with  $m$ . Scheme [19] proposes a new multi-authority attribute-based encryption system. In their system, any party can become an authority and there is no requirement for any global coordination other than the creation of an initial set of common reference parameters. Reference [20] gave attribute-based threshold signature scheme without a trusted central authority.

## II. PRELIMINARIES

In this section, we give the related preliminaries:

### Definition. *k*-Sibling Intractable Function Families

Let  $k = k(n)$  be a polynomial with  $k \geq 1$ . Let  $H = \{H_n, n \in N\}$ , where  $H_n = \{h_n \mid h_n : \sum^{l(n)} \rightarrow \sum^{m(n)}\}$ , be a family of functions that is one-way, polynomial time computable and samplable, and that has the collision accessibility property. Also let  $X = \{x_1, x_2, \dots, x_i\}$  be any set of  $i$  initial strings, where  $1 \leq i \leq k$ .  $H$  is a  $k$ -sibling intractable function family, or simply  $k$ -SIFF, if for each  $1 \leq i \leq k$ , for each sibling finder  $F$ , for each polynomial  $Q$ , and for all sufficiently large  $n$ ,

$$\Pr\{F(X, h) \neq ?\} < \frac{1}{Q(n)} \quad (1)$$

Where  $h$  is chosen randomly and uniformly from  $H_n^X \subset H_n$  the set of all functions in  $H_n$  that map  $x_1, x_2, \dots, x_i$  to the same strings in  $\sum^{m(n)}$ , and the probability  $\Pr\{F(X, h) \neq ?\}$  is computed over  $H_n^X$  and the sample space of all finite strings of coin flips that  $F$  could have tossed.

To figure axis labels, use words rather than symbols. Do not label axes only with units. Do not label axes with a ratio of quantities and units. Figure labels should be legible, about 9-point type.

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## III. DEFINITION AND SECURITY MODEL

### A. Definition

Refer to certificateless public key cryptography introduced by Al-Riyami and Paterson [1], we give two definitions about the vary types of attribute-based encryption :

#### Definition 1. Ciphertext-Policy Attribute-Based Certificateless Encryption Scheme.

A generic ciphertext-policy attribute-based certificateless encryption scheme consists of the following seven algorithms:

**-SetUp:** a probabilistic polynomial time (PPT) algorithm run by a key generation center (KGC) given a security parameter  $k$  and a universe of attributes  $U$  as input which outputs a randomly chosen master secret key  $msk$  and master public key  $mpk$ . The master public key  $mpk$  includes a description of the message space  $M$  and ciphertext space  $C$ .

**-PartialPrivateKeyExtract:** given the master public key  $mpk$ , master secret key  $msk$  and an attributes set  $S \in U$  for entity  $A$ , the KGC runs this PPT algorithm to generate the partial private key  $d_A$  for the attributes

set  $S$ , Then the partial private key  $d_A$  is transported to entity  $A$  over a confidential and authentic channel.

**-SetSecretValue:** a PPT algorithm runs by the entity  $A$  given master public key  $mpk$  and his attributes set  $S \in U$  as inputs which output a secret value  $x_A$ .

**-SetPrivateKey:** given master public key  $mpk$ , the entity  $A$ 's secret value  $x_A$ , and the entity  $A$ 's partial private key  $d_A$  as input, the entity runs this PPT algorithm to generate a private key  $SK_A$ .

**-SetPublicKey:** given master public key  $mpk$  and the entity  $A$ 's secret value  $x_A$ , and output a public key  $PK_A$  for the entity  $A$ .

**-Encrypt:** given a plaintext  $m \in M$ , master public key  $mpk$ , an access tree  $T$  over the universe of attributes  $U$  and public keys list  $PK_{A_1}, PK_{A_2}, \dots, PK_{A_n}$  for an entity

$A_1, A_2, \dots, A_n$  as inputs, a sender runs this PPT algorithm to create a ciphertext  $c \in C$  or the null symbol  $\perp$  indicating an encryption failure.

**-Decrypt:** given master public key  $mpk$ , the entity's private key  $SK_A$ , and the ciphertext  $c \in C$  that was encrypted under the access tree  $T$  as inputs, the entity as a recipient runs this deterministic algorithm to get a decryption  $\delta$ , which is a plaintext message if the set  $S$  of attributes satisfies the access tree  $T$ .

#### Definition 2. Key-Policy Attribute-Based Certificateless Encryption

The definition is similar to the ciphertext-policy attribute-based certificateless encryption scheme, and we omit here.

### B. Security Model

The following gives the security model for attribute-based certificateless encryption scheme:

In order to simulate the attack environment conveniently, we adopt the challenger  $C$  and adversary  $A$  model. Two kinds of adversaries are considered in the model. One is Type  $I$  adversary who cannot know the KGC's master secret key, but can replace any public key in publickeylist with other public keys he chooses. Another is Type  $II$  adversary who knows the KGC's master secret key and may still obtain full private keys for arbitrary attributes sets, but is disallowed to replace public key during the game.

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**Definition 3.** IND-CPA Secure against Type *I* Adversary for Ciphertext-Policy Attribute-Based Certificateless Encryption.

A ciphertext-policy attribute-based certificateless encryption scheme is IND-CPA secure against Type *I* adversary if no PPT adversary *A* of Type *I* has a non-negligible advantage in the following game played against the challenger:

- *A* is a Type *I* attacker, the challenger takes a security parameter *k* and runs the setup algorithm. It gives *A* the master public key *mpk*, and keeps the master secret key *msk* to itself.

- *A* is given access to the following oracles:

**-Public-Key-Request-Oracle:** with master public key *mpk* as input, *C* chooses a random *PK* in publickeylist and returns it.

**-Public-Key-Replace-Oracle:** with a valid public key *PK* as input, *C* replaces any one of the public key in publickeylist with *PK*.

**-Partial-Private-Key-Extract-Oracle:** with attributes set *S*, master public key *mpk*, and master secret key *msk* as input, *C* searches the PartialPrivateKeylist, and returns *d<sub>S</sub>*, if *S* is in the list. Else, he computes *d<sub>S</sub>* = PartialPrivateKeyExtract (*mpk*, *msk*, *S*), adds *<S, d<sub>S</sub>>* to PartialPrivateKey list and returns it to *A*.

**-Secret-Value-Extract-Oracle:** with a public key *PK* as input, *C* returns the corresponding secret value *x*.

- After making the oracle queries a polynomial number of times, *A* outputs and submits two messages (*M<sub>0</sub>*, *M<sub>1</sub>*), together with a challenge access tree *T*. The challenger *C* picks a random bit *b* ∈ {0,1} and computes *c*, the encryption of *M<sub>b</sub>*, for the current publickeylist and access tree *T*. If the output of the encryption is ⊥, then *A* immediately losses the game. Otherwise *C* is delivered to *A*.

- *A* makes a new sequence of queries as in step 2.

- *A* outputs a bit *b*. It wins if *b'* = *b* and fulfills the following conditions:

- At any time, the set *S* satisfying the access tree *T* has not been queried in -Partial-Private-Key-Extract-Oracle with any query of -Public-Key-Replace-Oracle.

Define the guessing advantage of *A* as

$$Adv_{ABCE}^{IND-CPA}(A) | \Pr[b' = b] - \frac{1}{2} | \quad (2)$$

A Type *I* adversary *A* breaks an IND-CPA secure ABCE scheme with (*t, q<sub>par</sub>, q<sub>pub</sub>, q<sub>sv</sub>, q<sub>pp</sub>, ε*) if and only if the guessing advantage of *A* that accesses *q<sub>par</sub>* times Partial-Private-Key-Extract-Oracle, *q<sub>pub</sub>* times Public-Key-Request-Oracle, *q<sub>sv</sub>* times Secret-Value-Extract-Oracle and *q<sub>pp</sub>* times Public-Key-Replace-Oracle is greater than *ε* within running time *t*. The scheme is said to be (*t, q<sub>par</sub>, q<sub>pub</sub>, q<sub>sv</sub>, q<sub>pp</sub>, ε*) -IND-CPA secure against Type *I* adversary if there is no

adversary *A* that can break the IND-CPA secure with (*t, q<sub>par</sub>, q<sub>pub</sub>, q<sub>sv</sub>, q<sub>pp</sub>, ε*).

**Definition 4.** IND-CPA Security against Type *II* Adversary for Ciphertext-Policy Attribute-Based Certificateless Encryption.

A ciphertext-policy attribute-based certificateless encryption scheme is IND-CPA secure against Type *II* adversary if no PPT adversary *A* of Type *II* has a non-negligible advantage in the following game played against the challenger:

- *A* is a Type *II* adversary, the challenger *C* run *A* with a security parameter *k* to get the master public key *mpk* and the master secret key *msk* to itself.

- *A* is given access to the following oracles:

**-Public-Key-Request-Oracle:** with master public key *mpk* as input, *C* chooses a random *PK* in publickeylist and returns it.

**-Secret-Value-Extract-Oracle:** with a public key *PK* as input, *C* returns the corresponding secret value *x*.

- After making the oracle queries a polynomial number of times, *A* outputs and submits two messages (*M<sub>0</sub>*, *M<sub>1</sub>*), together with a challenge access tree *T*. The challenger *C* picks a random bit *b* ∈ {0,1} and computes the encryption of *M<sub>b</sub>* for the current publickeylist and access tree *T*. If the output of the encryption is ⊥, then *A* immediately losses the game. Otherwise *c* is delivered to *A*.

- *A* makes a new sequence of queries as in step 2.

- *A* outputs a bit *b*. It wins if *b'* = *b* and fulfills the following conditions:

- At any time, any public key in the current publickeylist has not been submitted to the Secret-Value-Extract-Oracle.

Define the guessing advantage of *A* as

$$Adv_{ABCE}^{IND-CPA}(A) | \Pr[b' = b] - \frac{1}{2} | \quad (3)$$

A Type *II* adversary *A* breaks an IND-CPA secure ABCE scheme with (*t, q<sub>pub</sub>, q<sub>sv</sub>, ε*) if and only if the guessing advantage of *A* that accesses *q<sub>pub</sub>* times Public-Key-Request-Oracle, *q<sub>sv</sub>* times Secret-Value-Extract-Oracle and is greater than *ε* within running time *t*. The scheme is said to be (*t, q<sub>pub</sub>, q<sub>sv</sub>, ε*) -IND-CPA secure against Type *II* adversary if there is no adversary *A* that can break the IND-CPA secure with (*t, q<sub>pub</sub>, q<sub>sv</sub>, ε*)

## IV. A GENERIC CONSTRUCTION

### A. The Construction

Let (*Setup'*; *Privatekey'*; *Encrypt'*; *Decryption'*) be an IND-CPA secure attribute-based encryption scheme, and (*G, E, D*) is an IND-CPA secure public key encryption scheme. Let (*SetUp*; *PartialPrivateKeyExtract*; *SetSec*; *SetPriv*; *SetPub*; *Encrypt*; *Decrypt*) be the attribute-based

certificateless encryption scheme from the above attribute-based encryption scheme and the public key encryption scheme, and the construction is as follows:

**-SetUp:** run *Setup'* of attribute-based encryption scheme to get the master secret key *msk* and master public key *mpk*. The master public key *mpk* includes a description of the ciphertext space *C*.

**-PartialPrivateKeyExtract:** given the master public key *mpk*, master secret key *msk* and an attributes set  $S \in U$  for entity *A*, the KGC runs this PPT algorithm *Privatekey'* to generate the partial private key  $d_A$  for the attributes set. Then the partial private key  $d_A$  is transported to entity *A* over a confidential and authentic channel.

**-SetSec:** run *G* *n* times to get the corresponding secret values  $x_1, x_2, \dots, x_n$  and public keys  $pk_1, pk_2, \dots, pk_n$ , assuming that there are *n* users. Especially,  $pk_i$  includes a description of the message space *M*.

**-SetPriv:** the private key  $SK_A$  for entity *A* is composed of the secret value  $x_A$ , and the entity *A*'s partial private key  $d_A$ .

**-SetPub:** The public key  $PK_A$  for the entity *A* is obtained from scheme of SetSec. The system public key is composed of  $(mpk, pk_1, pk_2, \dots, pk_n)$ .

**-Encrypt:** given a plaintext  $m \in M$ , the ciphertext is  $c = Encryption'(E_{pk_1}(m) || E_{pk_2}(m) || \dots || E_{pk_n}(m))$  (4)

**-Decrypt:** given master public key *mpk*, the entity's private key  $SK_A = (d_A, x_A)$ , and the ciphertext  $c \in C$ , if entity's attributes set satisfying the access tree *T* related with *c* (ciphertext-policy attribute-based encryption scheme), or the attributes related with *c* satisfies the access tree *T* (key-policy attribute-based encryption scheme), and then he can get the message as follows:

$$m = D_{x_A}(Decryption'_{d_A}(c)) \quad (5)$$

Otherwise outputs  $\perp$ .

*B. Security Analysis*

**Theorem 1.** Our ciphertext-policy attribute-based certificateless encryption scheme is at least as secure as the attribute-based encryption scheme or the public key encryption scheme considering Type *I* adversary.

**Proof:** Assuming  $A_1$  is the Type *I* adversary, and then we can construct an attacker  $B_1$  for attribute-based encryption scheme or an attacker  $B_2$  for public key encryption scheme. Our idea is as follows:  $B_1$  or  $B_2$  simulates the attack environment of  $A_1$  until he attacks attribute-based encryption scheme or public key encryption scheme successively by running  $A_1$ .

Case 1: Attribute-based encryption scheme is IND-CPA secure.

**Setup:** Given the master public keys,  $B_1$  runs public key scheme *n* times to get *n* public-secret key pairs

$(pk_i, sk_i), (i = 1, 2, \dots, n)$ , and sends  $pk_i$ , with the master public keys *mpk* to  $A_1$ ,

**Phase 1.**  $B_1$  answers the queries of  $A_1$  as follows:

**-Public-Key-Request-Oracle:** On receiving the query:

1.  $B_1$  firstly searches PublicKeylist for a public key and returns it.
2. Else, he runs public key scheme to get public-secret key pair  $(pk_i, sk_i)$  and returns  $pk_i$  as answer.

**-Public-Key-Replace-Oracle:** On receiving a query  $pk$ ,  $B_1$  replaces any public key in publickeylist with  $pk$

**-Partial-Private-Key-Request-Oracle:** On receiving a query  $S \in U$ :

1.  $B_1$  Searches the PartialPrivateKey List for a tuple  $\langle S, d_A \rangle$  If exist, he returns  $d_A$  as answer.
2. Otherwise,  $B_1$  queries the challenge *C* for *S* in partial-private-key-request-oracle to get  $d_A$  and returns it.

**-Secret-Value-Extract-Oracle:** with a public key  $pk$  as input, *C* returns the corresponding secret value *x*.

**-Challenge:** After making the oracle queries a polynomial number of times,  $A_1$  outputs and submits two messages  $(M_0, M_1)$ , together with a challenge access tree *T*,  $B_1$  sends  $M_0 = (E_{pk_1}(m_0) || E_{pk_2}(m_0) || \dots || E_{pk_n}(m_0))$   
 $M_1 = (E_{pk_1}(m_1) || E_{pk_2}(m_1) || \dots || E_{pk_n}(m_1))$  to challenger *C*, *C* picks a random bit  $b \in \{0,1\}$  and computes *c*, the encryption of  $M_b$  for the current publickeylist and access tree *T*. If the output of the encryption is  $\perp$ , then  $B_1$  immediately losses the game. Otherwise *c* is delivered to  $B_1$  and  $B_1$  returns it to  $A_1$ .

**Phase 2.**  $A_1$  makes a new sequence of queries as in step 2, and  $B_1$  answer it as phase 1.

$A_1$  outputs a bit *b* and  $B_1$  outputs  $b'$ . It wins if  $b' = b$  and fulfills the following conditions:

- At any time, the set *S* satisfying the access tree *T* has not been queried in -Partial-Private-Key-Extract-Oracle with any query of -Public-Key-Replace-Oracle.

From the above analysis, we found, the successful probability of  $B_1$  is at least the same to the successful probability of  $A_1$ .

Case 2. If public key encryption scheme is IND-CPA secure, and the attribute-based encryption scheme is not IND-CPA secure. We can prove the successful probability of  $B_2$  attacking the public key encryption is at least the same to  $A_1$  in the light of the above proof method.

The attribute-based certificateless encryption scheme is IND-CPA secure against type  $\mathcal{II}$  adversary can be proved by the following theorem.

**Theorem 2.** If the public key encryption scheme is IND-CPA secure, then our ciphertext-policy attribute-based certificateless encryption scheme is IND-CPA secure against Type  $\mathcal{II}$  adversary.

The security analysis for key-policy attribute-based certificateless encryption scheme is similar to the one of ciphertext-policy attribute-based certificateless encryption scheme.

## V. IMPROVEMENT

The scheme from the above section is fit for the small universe of attributes or small group of users. If there are larger universe of attributes or more potential users, the scheme has lower efficiency due to the encryption scheme and more public keys. In this section, we improve on the above attribute-based certificateless encryption scheme by using of  $k$ -sibling intractable function families and one-way trapdoor function family.

Let  $(Setup', Privatekey', Encryption', Decryption')$  be an IND-CPA secure attribute-based encryption scheme,  $H = \{H_n, n \in N\}$  be a  $k$ -sibling intractable function family, where  $H_n = \{h_n | h_n : \sum^{l(n)} \rightarrow \sum^{m(n)}\}$ .  $G = \{G_n, n \in N\}$  be a pseudo-random function families, where  $G_n = \{g_n | g_n : \sum^{l(n)} \rightarrow \sum^{m(n)}\}$  and  $F = \{F_n, n \in N\}$  be a one-way trapdoor function family, where  $F_n = \{f_n | f_n : \sum^{l(n)} \rightarrow \sum^{m(n)}\}$ . Let  $(Setup; PartialPrivateKeyExtract; SetSec; SetPriv; SetPub; Encrypt; Decrypt)$  be the attribute-based certificateless encryption scheme,  $k$ -sibling intractable function families and one-way trapdoor function, and the construction is as follows:

**-SetUp:** run  $Setup'$  of attribute-based encryption scheme to get the master secret key  $msk$  and master public key  $mpk$ . The master public key  $mpk$  includes a description of the ciphertext space  $C$ .

**-PartialPrivateKeyExtract:** given the master public key  $mpk$ , master secret key  $msk$  and an attributes set  $S_i \in U$  for entity  $A_i$ , the KGC runs this PPT algorithm  $Privatekey'$  to generate the partial private key  $d_{A_i}$  for the attributes set. Then the partial private key  $d_{A_i}$  is transported to entity  $A_i$  over a confidential and authentic channel.

**-SetSec:** given master public key  $mpk$  and his attributes set  $S_i \in U$  as inputs, entity  $A_i$  outputs a secret value  $x_{A_i}$ .

For all  $A_i$ ,  $(i = 1, 2, \dots, n)$  he computes  $y_i = g_{x_{A_i}}(S_i)$ ,  $(i = 1, 2, \dots, n)$ , then all the entities jointly

get a  $k$ -sibling intractable function  $h$  satisfying  $h(y_i) = x$ ,  $(i = 1, 2, \dots, n)$ .

**-SetPriv:** given master public key  $mpk$ , the entity  $A_i$ 's secret value  $x_{A_i}$  and temporary secret key  $x$ , and the entity  $x_{A_i}$ 's partial private key  $d_{A_i}$  as input, the entity runs this PPT algorithm to generate a private key  $SK_{A_i}$ .

**-SetPub:** given master public key  $mpk$  and the entity  $A_i$ 's secret value  $x_{A_i}$ , one-way trapdoor function  $f$  with  $x$  as its trapdoor is returned.

**-Encrypt:** given a plaintext  $m \in M$ , the ciphertext is

$$c = Encrypt'(f(m)) \quad (6)$$

**-Decrypt:** given master public key  $mpk$ , the entity's Private Key  $SK_{A_i} = (d_{A_i}, x_{A_i})$  and the ciphertext  $c \in C$ .

If entity's attributes set satisfying the access tree  $T$  related with  $c$  (ciphertext-policy attribute-based encryption scheme), or the attributes related with  $c$  satisfies the access tree  $T$  (key-policy attribute-based encryption scheme), and then he can get the message as follows:

$$m = f_x^{-1}(Decrypt'_{d_A}(c)) \quad (7)$$

Otherwise outputs  $\perp$ .

## VI. CONCLUSIONS

In this paper, we give the new definition for attribute-based certificateless encryption scheme, and a generic construction is presented. The security of the generic construction is at least the same as the attribute-based encryption scheme. Of course, in order to give IND-CCA secure scheme, we can depend on weaker attribute-based encryption scheme, which is our further research. In order to improve the efficiency of attribute-based certificateless encryption scheme, we get an improvement by using a  $k$ -sibling intractable function family, and the improvement has shorter public key and efficient encryption and decryption scheme. Furthermore, our scheme is fit for key updating when there are users changed.

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